**Topics: Normal distribution, Functions of Random Variables**

1. The time required for servicing transmissions is normally distributed with *μ* = 45 minutes and *σ* = 8 minutes. The service manager plans to have work begin on the transmission of a customer’s car 10 minutes after the car is dropped off and the customer is told that the car will be ready within 1 hour from drop-off. What is the probability that the service manager cannot meet his commitment?
2. 0.3875
3. 0.2676
4. 0.5
5. 0.6987
6. The current age (in years) of 400 clerical employees at an insurance claims processing center is normally distributed with mean *μ* = 38 and Standard deviation *σ* =6. For each statement below, please specify True/False. If false, briefly explain why.
7. More employees at the processing center are older than 44 than between 38 and 44.
8. A training program for employees under the age of 30 at the center would be expected to attract about 36 employees.

**Ans:**

1. p(X>44) = 0.1587

p(38<X<44) = 0.3413

**The statement is False.** The Probability of employees aged from 38 to 44 is more.

1. N\*P(X<30) = 36.49

**The statement is true.** The no. of employees aged below 30 years attending training is 36.

1. If *X1* ~ *N*(μ, σ2) and *X*2 ~ *N*(μ, σ2) are *iid* normal random variables, then what is the difference between 2 *X*1 and *X*1 + *X*2? Discuss both their distributions and parameters.

**Ans: 2X1 = N(2μ, 4σ2)** and **X1 + X2 = N(2μ, σ2)**

From above calculations we can say that spread of data range in 1st case is 4 times that of 2nd case whereas mean in both cases are same.

1. Let X ~ N(100, 202). Find two values, *a* and *b*, symmetric about the mean, such that the probability of the random variable taking a value between them is 0.99.
2. 90.5, 105.9
3. 80.2, 119.8
4. 22, 78
5. **48.5, 151.5**
6. 90.1, 109.9

**Ans:**

Interval For probability of 0.99 is,

stats.norm.interval(0.99,100,20) = **(48.48, 151.51)**

1. Consider a company that has two different divisions. The annual profits from the two divisions are independent and have distributions Profit1 ~ N(5, 32) and Profit2 ~ N(7, 42) respectively. Both the profits are in $ Million. Answer the following questions about the total profit of the company in Rupees. Assume that $1 = Rs. 45
2. Specify a Rupee range (centered on the mean) such that it contains 95% probability for the annual profit of the company.
3. Specify the 5th percentile of profit (in Rupees) for the company
4. Which of the two divisions has a larger probability of making a loss in a given year?

**Ans:**

1. The Range for 95% probability for the annual profit of the company is Rs.99 to 981 Million.
2. The 5th percentile of profit for the company is Rs.170 Million.
3. P(X1) = 4.78 % & P(X2) = 4 %

Probability of Division 1 making a loss in a given year is more than Division 2.